## Probability Rules

- Sensitivity: probability that a test or procedure result will be positive when the disease is present.
- Specificity: probability that a test or procedure result will be negative when the disease is not present.
- True Positive Rate: sensitivity (in percent)
- False Positive Rate: probability that a test or procedure result will be positive when the disease is not present. [100 minus specificity (in percent)]
- True Negative Rate: specificity (in percent)
- False Negative Rate: probability that a test or procedure result will be negative when the disease is present. [100 minus sensitivity (in percent)]
- Positive Predictive Value: probability that the disease is present when the test or procedure result is positive.
- Negative Predictive Value: probability that the disease is not present when the test or procedure result is negative.

A common test for AIDS is called the ELISA test. Among 1,000,000 people who are given the ELISA test, we can expect results similar to those given in the table.

|  | $B_{1}:$ Carry <br> AIDS <br> Virus | $B_{2}:$ Do Not <br> Carry AIDS <br> Virus |  |
| :---: | ---: | ---: | ---: |
| $A_{1}:$ Test Positive | 4,885 | 73,630 | 78,515 |
| $A_{2}:$ Test Negative | 115 | 921,370 | 921,485 |
| Totals | 5,000 | 995,000 | $1,000,000$ |

If one of these $1,000,000$ people is selected randomly, find the following probabilities and interpret

1. $P\left(B_{1}\right)$
2. $P\left(A_{1}\right)$
3. $P\left(A_{1}\right.$ given that $B_{2}$ has occurred $)$
4. $P\left(B_{2}\right.$ given that $A_{1}$ has occurred $)$
5. $P\left(B_{1}\right.$ given that $A_{1}$ has occurred $)$
6. $P\left(A_{1}\right.$ given that $B_{1}$ has occurred $)$
7. $P\left(A_{2}\right.$ given that $B_{2}$ has occurred $)$
8. $P\left(A_{2}\right.$ given that $B_{1}$ has occurred $)$
9. $P\left(B_{2}\right.$ given that $A_{2}$ has occurred $)$

|  |  | True State |  |
| :---: | :---: | :---: | :---: |
|  | No Virus | Virus |  |
|  | Positive <br> test | Type I <br> Error | Corrrect <br> Decision |
| Negative <br> test | Correct <br> Decision | Type II <br> Error |  |

